

Third Grade Pacing Guide

Vision Statement

Imagine a classroom, a school, or a school district where all students have access to high-quality, engaging mathematics instruction. There are ambitious expectations for all, with accommodation for those who need it. Knowledgeable teachers have adequate resources to support their work and are continually growing as professionals. The curriculum is mathematically rich, offering students opportunities to learn important mathematical concepts and procedures with understanding. Technology is an essential component of the environment. Students confidently engage in complex mathematical tasks chosen carefully by teachers. They draw on knowledge from a wide variety of mathematical topics, sometimes approaching the same problem from different mathematical perspectives or representing the mathematics in different ways until they find methods that enable them to make progress. Teachers help students make, refine, and explore conjectures on the basis of evidence and use a variety of reasoning and proof techniques to confirm or disprove those conjectures. Students are flexible and resourceful problem solvers. Alone or in groups and with access to technology, they work productively and reflectively, with the skilled guidance of their teachers. Orally and in writing, students communicate their ideas and results effectively. They value mathematics and engage actively in learning it.

National Council of Teachers of Mathematics

Process Standards

Mathematical Problem Solving

Students will apply mathematical concepts and skills and the relationships among them to solve problem situations of varying complexities. Students also will recognize and create problems from real-life data and situations within and outside mathematics and then apply appropriate strategies to find acceptable solutions. To accomplish this goal, students will need to develop a repertoire of skills and strategies for solving a variety of problem types. A major goal of the mathematics program is to help students become competent mathematical problem solvers.

Mathematical Communication

Students will use the language of mathematics, including specialized vocabulary and symbols, to express mathematical ideas precisely. Representing, discussing, reading, writing, and listening to mathematics will help students to clarify their thinking and deepen their understanding of the mathematics being studied.

Mathematical Reasoning

Students will recognize reasoning and proof as fundamental aspects of mathematics. Students will learn and apply inductive and deductive reasoning skills to make, test, and evaluate mathematical statements and to justify steps in mathematical procedures. Students will use logical reasoning to analyze an argument and to determine whether conclusions are valid. In addition, students will learn to apply proportional and spatial reasoning and to reason from a variety of representations such as graphs, tables, and charts.

Mathematical Connections

Students will relate concepts and procedures from different topics in mathematics to one another and see mathematics as an integrated field of study. Through the application of content and process skills, students will make connections between different areas of mathematics and between mathematics and other disciplines, especially science. Science and mathematics teachers and curriculum writers are encouraged to develop mathematics and science curricula that reinforce each other.

Mathematical Representations

Students will represent and describe mathematical ideas, generalizations, and relationships with a variety of methods. Students will understand that representations of mathematical ideas are an essential part of learning, doing, and communicating mathematics. Students should move easily among different representations—graphical, numerical, algebraic, verbal, and physical—and recognize that representation is both a process and a product.

Strand: Number and Number Sense

Students in grades K–3 have a natural curiosity about their world, which leads them to develop a sense of number. Young children are motivated to count everything around them and begin to develop an understanding of the size of numbers (magnitude), multiple ways of thinking about and representing numbers, strategies and words to compare numbers, and an understanding of the effects of simple operations on numbers. Building on their own intuitive mathematical knowledge, they also display a natural need to organize things by sorting, comparing, ordering, and labeling objects in a variety of collections.

Consequently, the focus of instruction in the number and number sense strand is to promote an understanding of counting, classification, whole numbers, place value, fractions, number relationships (“more than,” “less than,” and “equal to”), and the effects of single-step and multistep computations. These learning experiences should allow students to engage actively in a variety of problem solving situations and to model numbers (compose and decompose), using a variety of manipulatives. Additionally, students at this level should have opportunities to observe, to develop an understanding of the relationship they see between numbers, and to develop the skills to communicate these relationships in precise, unambiguous terms.

Strand: Computation and Number Sense

A variety of contexts are necessary for children to develop an understanding of the meanings of the operations such as addition and subtraction. These contexts often arise from real-life experiences in which they are simply joining sets, taking away or separating from a set, or comparing sets. These contexts might include conversations, such as “How many books do we have altogether?” or “How many cookies are left if I eat two?” or “I have three more candies than you do.” Although young children first compute using objects and manipulatives, they gradually shift to performing computations mentally or using paper and pencil to record their thinking. Therefore, computation and estimation instruction in the early grades revolves around modeling, discussing, and recording a variety of problem situations. This approach helps students transition from the concrete to the representation to the symbolic in order to develop meaning for the operations and how they relate to each other.

In grades K–3, computation and estimation instruction focuses on

- relating the mathematical language and symbolism of operations to problem situations;
- understanding different meanings of addition and subtraction of whole numbers and the relation between the two operations;
- developing proficiency with basic addition, subtraction, multiplication, division and related facts;
- gaining facility in manipulating whole numbers to add and subtract and in understanding the effects of the operations on whole numbers;
- developing and using strategies and algorithms to solve problems and choosing an appropriate method for the situation;
- choosing, from mental computation, estimation, paper and pencil, and calculators, an appropriate way to compute;
- recognizing whether numerical solutions are reasonable;
- experiencing situations that lead to multiplication and division, such as equal groupings of objects and sharing equally; and
- performing initial operations with fractions.

Strand: Measurement

Measurement is important because it helps to quantify the world around us and is useful in so many aspects of everyday life. Students in grades K–3 should encounter measurement in many normal situations, from their daily use of the calendar and from science activities that often require students to measure objects or compare them directly, to situations in stories they are reading and to descriptions of how quickly they are growing.

Measurement instruction at the primary level focuses on developing the skills and tools needed to measure length, weight/mass, capacity, time, temperature, area, perimeter, volume, and money. Measurement at this level lends itself especially well to the use of concrete materials. Children can see the usefulness of measurement if classroom experiences focus on estimating and measuring real objects. They gain deep understanding of the concepts of measurement when handling the materials, making physical comparisons, and measuring with tools.

As students develop a sense of the attributes of measurement and the concept of a measurement unit, they also begin to recognize the differences between using nonstandard and standard units of measure. Learning should give them opportunities to apply both techniques and nonstandard and standard tools to find measurements and to develop an understanding of the use of simple U.S. Customary and metric units.

Teaching measurement offers the challenge to involve students actively and physically in learning and is an opportunity to tie together other aspects of the mathematical curriculum, such as fractions and geometry. It is also one of the major vehicles by which mathematics can make connections with other content areas, such as science, health, and physical education.

Strand: Geometry

Children begin to develop geometric and spatial knowledge before beginning school, stimulated by the exploration of figures and structures in their environment. Geometric ideas help children systematically represent and describe their world as they learn to represent plane and solid figures through drawing, block constructions, dramatization, and verbal language.

The focus of instruction at this level is on

- observing, identifying, describing, comparing, contrasting, and investigating solid objects and their faces;
- sorting objects and ordering them directly by comparing them one to the other;
- describing, comparing, contrasting, sorting, and classifying figures; and
- exploring symmetry, congruence, and transformation.

In the primary grades, children begin to develop basic vocabulary related to figures but do not develop precise meanings for many of the terms they use until they are thinking beyond Level 2 of the van Hiele theory (see below).

The van Hiele theory of geometric understanding describes how students learn geometry and provides a framework for structuring student experiences that should lead to conceptual growth and understanding.

- **Level 0: Pre-recognition.** Geometric figures are not recognized. For example, students cannot differentiate between three-sided and four-sided polygons.
- **Level 1: Visualization.** Geometric figures are recognized as entities, without any awareness of parts of figures or relationships between components of a figure. Students should recognize and name figures and distinguish a given figure from others that look somewhat the same. (This is the expected level of student performance during grades K and 1.)
- **Level 2: Analysis.** Properties are perceived but are isolated and unrelated. Students should recognize and name properties of geometric figures. (Students are expected to transition to this level during grades 2 and 3.)

Strand: Probability and Statistics

Students in the primary grades have a natural curiosity about their world, which leads to questions about how things fit together or connect. They display their natural need to organize things by sorting and counting objects in a collection according to similarities and differences with respect to given criteria.

The focus of probability instruction at this level is to help students begin to develop an understanding of the concept of chance. They experiment with spinners, two-colored counters, dice, tiles, coins, and other manipulatives to explore the possible outcomes of situations and predict results. They begin to describe the likelihood of events, using the terms *impossible*, *unlikely*, *equally likely*, *more likely*, and *certain*.

The focus of statistics instruction at this level is to help students develop methods of collecting, organizing, describing, displaying, and interpreting data to answer questions they have posed about themselves and their world.

Strand: Patterns, Functions, and Algebra

Stimulated by the exploration of their environment, children begin to develop concepts related to patterns, functions, and algebra before beginning school. Recognition of patterns and comparisons are important components of children's mathematical development.

Students in kindergarten through third grade develop the foundation for understanding various types of patterns and functional relationships through the following experiences:

- sorting, comparing, and classifying objects in a collection according to a variety of attributes and properties;
- identifying, analyzing, and extending patterns;
- creating repetitive patterns and communicating about these patterns in their own language;
- analyzing simple patterns and making predictions about them;
- recognizing the same pattern in different representations;
- describing how both repeating and growing patterns are generated; and
- repeating predictable sequences in rhymes and extending simple rhythmic patterns.

The focus of instruction at the primary level is to observe, recognize, create, extend, and describe a variety of patterns. These students will experience and recognize visual, kinesthetic, and auditory patterns and develop the language to describe them orally and in writing as a foundation to using symbols. They will use patterns to explore mathematical and geometric relationships and to solve problems, and their observations and discussions of how things change will eventually lead to the notion of functions and ultimately to algebra.

Quarterly Overview Sheet

1 st Quarter	2 nd Quarter	3 rd Quarter	4 th Quarter
<p>Strand: Number and Number Sense Focus: Place Value and Fractions</p> <p>3.1 The student will</p> <ol style="list-style-type: none"> a) read and write six-digit numerals and identify the place value and value of each digit; b) round whole numbers, 9,999 or less, to the nearest ten, hundred, and thousand; and c) compare two whole numbers between 0 and 9,999, using symbols (>, <, or =) and words (<i>greater than</i>, <i>less than</i>, or <i>equal to</i>). <p>Strand: Patterns, Functions, and Algebra Focus: Patterns and Property Concepts</p> <p>3.20 The student will</p> <ol style="list-style-type: none"> a) investigate the identity and the commutative properties for addition b) identify examples of the identity and commutative properties for addition <p>Strand: Number and Number Sense Focus: Place Value and Fractions</p> <p>3.2 The student will recognize and use the inverse relationships between addition/subtraction to complete basic fact sentences. The student will use these relationships to solve problems.</p> <p>Strand: Computation and Estimation Focus: Computation and Fraction Operation</p> <p>3.4 The student will estimate solutions to and solve single-step and multistep problems involving the sum or difference of two whole numbers, each 9,999 or less, with or without regrouping.</p> <p>Strand: Probability and Statistics Focus: Application of Data and Chance</p> <p>3.17 The student will</p> <ol style="list-style-type: none"> a) collect and organize data, using observations, measurements, surveys, or experiments; b) construct a line plot, a picture graph, or a bar graph to represent the data; and c) read and interpret the data represented in line plots, bar graphs, and picture 	<p>Strand: Patterns, Functions, and Algebra Focus: Patterns and Property Concepts</p> <p>3.19 The student will recognize and describe a variety of patterns formed using numbers, tables, and pictures, and extend the patterns, using the same or different forms.</p> <p>3.20 The student will</p> <ol style="list-style-type: none"> a) investigate the identity and the commutative properties for multiplication; b) identify examples of the identity and commutative properties for multiplication. <p>Strand: Number and Number Sense Focus: Place Value and Fractions</p> <p>3.2 The student will recognize and use the inverse relationships between multiplication/division to complete basic fact sentences. The student will use these relationships to solve problems.</p> <p>Strand: Computation and Estimation Focus: Computation and Fraction Operation</p> <p>3.5 The student will recall multiplication facts through the twelves table, and the corresponding division facts.</p> <p>3.6 The student will represent multiplication and division, using area, set, and number line models, and create and solve problems that involve multiplication of two whole numbers, one factor 99 or less and the second factor 5 or less.</p> <p>Strand: Number and Number Sense Focus: Place Value and Fractions</p> <p>3.3 The student will</p> <ol style="list-style-type: none"> a) name and write fractions (including mixed numbers) represented by a model; b) model fractions (including mixed numbers) and write the fractions' names; c) compare fractions having like and unlike denominators, using words and symbols (>, <, or =). <p>Strand: Computation and Estimation Focus: Computation and Fraction Operation</p> <p>3.7 The student will add and subtract proper</p>	<p>Strand: Measurement Focus: US Customary and Metric Units, Area and Perimeter, and Time</p> <p>3.11 The student will</p> <ol style="list-style-type: none"> a) tell time to the nearest minute, using analog and digital clocks; and b) determine elapsed time in one-hour increments over a 12-hour period. <p>3.12 The student will identify equivalent periods of time, including relationships among days, months, and years, as well as minutes and hours.</p> <p>3.8 The student will determine, by counting, the value of a collection of bills and coins whose total value is \$5.00 or less, compare the value of the bills and coins, and make change.</p> <p>3.9 The student will estimate and use U.S. Customary and metric units to measure</p> <ol style="list-style-type: none"> a) length to the nearest $\frac{1}{2}$ inch, inch, foot, yard, centimeter, and meter; b) liquid volume in cups, pints, quarts, gallons, and liters; c) weight/mass in ounces, pounds, grams, and kilograms; and d) area and perimeter. <p>3.10 The student will</p> <ol style="list-style-type: none"> a) measure the distance around a polygon in order to determine perimeter; and b) count the number of square units needed to cover a given surface in order to determine area. <p>3.13 The student will read temperature to the nearest degree from a Celsius thermometer and a Fahrenheit thermometer. Real thermometers and physical models of thermometers will be used.</p>	<p>Strand: Geometry Focus: Properties of congruence, characteristics of plane and solid figures.</p> <p>3.14 The student will identify, describe, compare, and contrast characteristics of plane and solid geometric figures (circle, square, rectangle, triangle, cube, rectangular prism, square pyramid, sphere, cone, and cylinder) by identifying relevant characteristics, including the number of angles, vertices, and edges, and the number and shape of faces, using concrete models.</p> <p>3.15 The student will identify and draw representations of points, line segments, rays, angles, and lines.</p> <p>3.16 The student will identify and describe congruent and noncongruent plane figures.</p> <p>Strand: Patterns, Functions, and Algebra Focus: Patterns and Property Concepts</p> <p>3.19 The student will recognize and describe a variety of patterns formed using numbers, tables, and pictures, and extend the patterns, using the same or different forms.</p> <p>Strand: Probability and Statistics Focus: Application of Data and Chance</p> <p>3.18 The student will investigate and describe the concept of probability as chance and list possible results of a given situation.</p>

graphs and write a sentence analyzing the data.

fractions having like denominators of 12 or less.

1st Quarter

Topic: Number and Number Sense

Focus: Place Value and Fractions

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.1 The student will

- read and write six-digit numerals and identify the place value and value of each digit;
- round whole numbers, 9,999 or less, to the nearest ten, hundred, and thousand; and
- compare two whole numbers between 0 and 9,999, using symbols ($>$, $<$, or $=$) and words (*greater than*, *less than*, or *equal to*).

Understanding the Standard Background information of teachers

- The structure of the Base-10 number system is based upon a simple pattern of tens, where each place is ten times the value of the place to its right. This is known as a ten-to-one place value relationship.
- The structure of the Base-10 blocks is based on the ten-to-one place value relationship (e.g., 10 units make a long, 10 longs make a flat, 10 flats make a cube).
- Place value refers to the value of each digit and depends upon the position of the digit in the number. In the number 7,864, the eight is in the hundreds place, and the value of the 8 is eight hundred.
- Flexibility in thinking about numbers — or “decomposition” of numbers (e.g., 12,345 is 123 hundreds, 4 tens, and 5 ones) — is critical and supports understandings essential to multiplication and division.
- Whole numbers may be written in a variety of formats:
 - Standard: 123,456;
 - Written: one hundred twenty-three thousand, four hundred fifty-six; and
 - Expanded: $(1 \times 100,000) + (2 \times 10,000) + (3 \times 1,000) + (4 \times 100) + (5 \times 10) + (6 \times 1)$.
- Numbers are arranged into groups of three places called *periods* (ones, thousands, millions, and so on). Places within the periods repeat (hundreds, tens, ones). Commas are used to separate the periods. Knowing the place value and period of a number helps students find the value of a digit in any number as well as read and write numbers.
- To read a whole number through the hundred thousands place,
 - read the digits to the first comma;
 - say the name of the period (e.g., “thousands”); then
 - read the last three digits, but do not say the name of the ones period.
- Reading and writing large numbers should be related to numbers that have meanings (e.g., numbers found in the students’ environment). Concrete materials, such as Base-10

blocks may be used to represent whole numbers through thousands. Larger numbers may be represented on place value charts.

- Rounding is one of the estimation strategies that is often used to assess the reasonableness of a solution or to give an estimate of an amount.
- Students should explore reasons for estimation, using practical experiences, and use rounding to solve practical situations.
- The concept of rounding may be introduced through the use of a number line. When given a number to round, locate it on the number line. Next, determine the multiple of ten, hundred, or thousand it is between. Then identify to which it is closer.
- A procedure for rounding numbers to the nearest ten, hundred, or thousand is as follows:
 - Look one place to the right of the digit to which you wish to round.
 - If the digit is less than 5, leave the digit in the rounding place as it is, and change the digits to the right of the rounding place to zero.
 - If the digit is 5 or greater, add 1 to the digit in the rounding place, and change the digits to the right of the rounding place to zero.
- A procedure for comparing two numbers by examining may include the following:
 - Line up the numbers by place value by lining up the ones.
 - Beginning at the left, find the first place value where the digits are different.
 - Compare the digits in this place value to determine which number is greater (or which is less).
 - Use the appropriate symbol $>$ or $<$ or the words *greater than* or *less than* to compare the numbers in the order in which they are presented.

If both numbers are the same, use the symbol $=$ or the words *equal to*.

Topic: Number and Number Sense

Focus: Place Value and Fractions

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.1 The student will

- a) read and write six-digit numerals and identify the place value and value of each digit;
- b) round whole numbers, 9,999 or less, to the nearest ten, hundred, and thousand; and
- c) compare two whole numbers between 0 and 9,999, using symbols ($>$, $<$, or $=$) and words (*greater than*, *less than*, or *equal to*).

Essential Knowledge and Skills	Essential Questions	Essential Understandings All Students should...	Tasks/ Recommended Activities
<p>Essential Vocabulary: Base-10 number system; place value; whole numbers; rounding; estimating; symbols $<$, $>$, or $=$; greater than; less than; equal to; digits;</p>			
<ul style="list-style-type: none"> • Investigate and identify the place and value for each digit in a six-digit numeral, using Base-10 manipulatives (e.g., Base-10 blocks). • Use the patterns in the place value system to read and write numbers. • Read six-digit numerals orally. • Write six-digit numerals that are stated verbally or written in words. • Round a given whole number, 9,999 or less, to the nearest ten, hundred, and thousand. • Solve problems, using rounding of numbers, 9,999 or less, to the nearest ten, hundred, and thousand. • Determine which of two whole numbers between 0 and 9,999 is greater. • Determine which of two whole numbers between 0 and 9,999 is less. • Compare two whole numbers between 0 and 9,999, using the symbols $>$, $<$, or $=$. 	<p>What is the position of a given number?</p> <p>What is the value of a given number?</p> <p>How are numbers related to each other?</p> <p>How would the following number be written in standard form (e.g., four hundred fifty)?</p> <p>How would this number ____ be rounded to the nearest ten? nearest hundred? Nearest thousand?</p> <p>What strategies can be used to read and compare large</p>	<p>All students should</p> <ul style="list-style-type: none"> • Understand that knowledge of place value is essential when comparing numbers. • Understand the relationships in the place value system, where each place is ten times the value of the place to its right. • Understand that rounding gives an estimate to use when exact numbers are not needed for the situation. • Understand the relative magnitude of numbers by comparing numbers. 	

<ul style="list-style-type: none">• Use the terms <i>greater than, less than, and equal to</i> when comparing two whole numbers.	<p>numbers?</p> <p>How are place value patterns repeated in large numbers?</p> <p>How do rounding and estimation help you to know if an answer is reasonable?</p> <p>How would you compare two numbers using $>$, $<$, $=$?</p> <p>How would you compare two numbers using greater than, less than, and equal to?</p> <p>Is it important to understand how numbers are related? Explain your answer.</p> <p>What is the value of 7 in 427,245?</p> <p>When rounding to the nearest hundred, why does 435 round to 400?</p> <p>What might happen if you combined 10,000 and 90,000?</p> <p>What is the value of 8 in 98,452?</p> <p>Why is 542 greater than 524?</p> <p>What might happen if you combined 80,000 and 20,000?</p>		
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Topic: Patterns, Functions, and Algebra

Focus: Patterns and Property Concepts

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.20 The student will

- a) investigate the identity and the commutative properties for addition ; and
- b) identify examples of the identity and commutative properties for addition.

Understanding the Standard Background information of teachers

- Investigating arithmetic operations with whole numbers helps students learn about several different properties of arithmetic relationships. These relationships remain true regardless of the numbers.
- The commutative property for addition states that changing the order of the addends does not affect the sum (e.g., $4 + 3 = 3 + 4$).
- The identity property for addition states that if zero is added to a given number, the sum is the same as the given number.
- A number sentence is an equation with numbers (e.g., $6 + 3 = 9$; or $6 + 3 = 4 + 5$).

Topic: Patterns, Functions, and Algebra

Focus: Patterns and Property Concepts

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard:3.20 The student will

- a) investigate the identity and the commutative properties for addition ; and
- b) identify examples of the identity and commutative properties for addition.

Essential Knowledge and Skills	Essential Questions	Essential Understandings All Students should...	Tasks/ Recommended Activities
<p>Essential Vocabulary: numeric patterns; commutative properties for addition; identity for addition; number sentence</p>			
<p>The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations to</p> <ul style="list-style-type: none"> • Investigate the identity property for addition and determine that when the number zero is added to another number or another number is added to the number zero, that number remains unchanged. Examples of the identity property for addition are $0 + 2 = 2$; $5 + 0 = 5$. • Recognize that the commutative property for addition is an order property. Changing the order of the addends does not change the sum ($5 + 4 = 9$ and $4 + 5 = 9$). • Write number sentences to represent equivalent mathematical relationships (e.g., $4 \times 3 = 14 - 2$). • Identify examples of the identity and commutative properties for addition. 	<p>What are effective methods for finding sums and differences?</p> <p>What is the commutative property for addition?</p> <p>What is the identity property of addition?</p> <p>How is equality defined?</p> <p>How does knowing the commutative and identity properties of addition help you solve problems?</p> <p>How can you determine if two sides of an equation are equal or not equal?</p> <p>Can you name a time when the identity property would not work?</p> <p>How does a mathematical expression show equivalent values? Explain your answer.</p>	<ul style="list-style-type: none"> • Understand that mathematical relationships can be expressed using number sentences. • Understand the identity property for addition. • Understand the commutative property of addition. • Understand that quantities on both sides of an equals sign must be equal. • Understand that quantities on both sides of the not equal sign are not equal. 	

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Topic: Number and Number Sense

Focus: Place Value and Fractions

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.2

The student will recognize and use the inverse relationships between addition/subtraction and to complete basic fact sentences. The student will use these relationships to solve problems.

Understanding the Standard Background information of teachers

- Addition and subtraction are inverse operations.
- In building thinking strategies for subtraction, an emphasis is placed on connecting the subtraction fact to the related addition fact. Building fact sentences helps strengthen this relationship.
- Addition and subtraction should be taught concurrently in order to develop understanding of the inverse relationship.

Topic: Number and Number Sense

Focus: Place Value and Fractions

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.2

The student will recognize and use the inverse relationships between addition/subtraction and to complete basic fact sentences. The student will use these relationships to solve problems.

Essential Knowledge and Skills	Essential Questions	Essential Understandings All Students should...	Tasks/ Recommended Activities
<p>Essential Vocabulary: place value; whole numbers; addition; subtraction; inverse operations</p>			
<p>The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations to</p> <ul style="list-style-type: none"> Use the inverse relationships between addition/subtraction to solve related basic fact sentences. For example, $5 + 3 = 8$ and $8 - 3 = \underline{\quad}$ Write three related basic fact sentences when given one basic fact sentence for addition/subtraction. For example, given $3 + 2 = 5$, solve the related facts $\underline{\quad} + 3 = 5$, $6 - 3 = \underline{\quad}$, and $3 + \underline{\quad} = 6$. 	<p>How do addition and subtraction relate to each other?</p> <p>What is an inverse relationship?</p> <p>What are efficient methods for finding sums and differences?</p> <p>Will knowing related addition and subtraction facts help you solve problems? Explain your answer.</p>	<ul style="list-style-type: none"> Understand how addition and subtraction are related. 	

Topic: Computation and Estimation

Focus: Computation and Fraction Operations

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.4

The student will estimate solutions to and solve single-step and multistep problems involving the sum or difference of two whole numbers, each 9,999 or less, with or without regrouping.

Understanding the Standard Background information of teachers

- Addition is the combining of quantities; it uses the following terms:
 - $addend \rightarrow 423$
 - $addend \rightarrow +246$
 - $sum \rightarrow 669$
- Subtraction is the inverse of addition; it yields the difference between two numbers and uses the following terms:
 - $minuend \rightarrow 7,698$
 - $subtrahend \rightarrow -5,341$
 - $difference \rightarrow 2,357$
- An algorithm is a step-by-step method for computing.
- An example of an approach to solving problems is Polya's four-step plan:
 - Understand: Retell the problem; read it twice; take notes; study the charts or diagrams; look up words and symbols that are new.
 - Plan: Decide what operation(s) and sequence of steps to use to solve the problem.
 - Solve: Follow the plan and work accurately. If the first attempt does not work, try another plan.
 - Look back: Does the answer make sense?
- Knowing whether to find an exact answer or to make an estimate is learned through practical experiences in recognizing which is appropriate.

- When an exact answer is required, opportunities to explore whether the answer can be determined mentally or must involve paper and pencil or calculators help students select the correct approach.
- Determining whether an estimate is appropriate and using a variety of strategies to estimate requires experiences with problem situations involving estimation.
- There are a variety of mental mathematics strategies for each basic operation, and opportunities to practice these strategies give students the tools to use them at appropriate times. For example, with addition, mental mathematics strategies include
 - Adding 9: add 10 and subtract 1; and
 - Making 10: for column addition, look for numbers that group together to make 10.
- Using Base-10 materials to model and stimulate discussion about a variety of problem situations helps students understand regrouping and enables them to move from the concrete to the abstract. Regrouping is used in addition and subtraction algorithms.
- Conceptual understanding begins with concrete experiences. Next, the children must make connections that serve as a bridge to the symbolic. One strategy used to make connections is representations, such as drawings, diagrams, tally marks, graphs, or written comments.

Topic: Computation and Estimation

Focus: Computation and Fraction Operations

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.4

The student will estimate solutions to and solve single-step and multistep problems involving the sum or difference of two whole numbers, each 9,999 or less, with or without regrouping.

Essential Knowledge and Skills	Essential Questions	Essential Understandings All Students should...	Tasks/ Recommended Activities
<p>Essential Vocabulary: addition; addend; sum; subtraction; minuend; subtrahend; difference; number line</p>			
<p>The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations to</p> <ul style="list-style-type: none"> • Determine whether an estimate or an exact answer is an appropriate solution for practical addition and subtraction problems situations involving single-step and multistep problems. • Determine whether to add or subtract in practical problem situations. • Estimate the sum or difference of two whole numbers, each 9,999 or less when an exact answer is not required. • Add or subtract two whole numbers, each 9,999 or less. • Solve practical problems involving the sum of two whole numbers, each 9,999 or less, with or without regrouping, using calculators, paper and pencil, or mental computation in practical problem situations. • Solve practical problems involving the difference of two whole numbers, each 9,999 or less, with or without regrouping, using calculators, paper and pencil, or 	<p>What are different models for addition and subtraction (partpart-whole, begin-change-end, join or separate)?</p> <p>What are the different methods to solve given problems?</p> <p>What strategies can be used to make a reasonable estimate?</p> <p>What information/strategy would you use to solve a multi-step word problem?</p> <p>How can knowing addition and subtraction facts help</p>	<ul style="list-style-type: none"> • Understand that estimation skills are valuable, time-saving tools particularly in practical situations when exact answers are not required or needed. • Understand that estimation skills are also valuable in determining the reasonableness of the sum or difference when solving for the exact answer is needed. • Develop and use strategies to estimate whole number sums and differences to determine the reasonableness of an exact answer. 	

<p>mental computation in practical problem situations.</p> <ul style="list-style-type: none"> • Solve single-step and multistep problems involving the sum or difference of two whole numbers, each 9,999 or less, with or without regrouping. 	<p>in solving problems? How can place value and decomposition of numbers be used to find sums and differences?</p> <p>How do you take apart and recombine numbers in a variety of ways for finding sums and differences?</p> <p>What computation tools are best suited to problem solve (objects, number line, mental math, pencil/paper)?</p>	<ul style="list-style-type: none"> • Develop flexible methods of adding whole numbers by combining numbers in a variety of ways, most depending on place values. 	
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Topic: Probability and Statistics

Focus: Application of Data and Chance

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

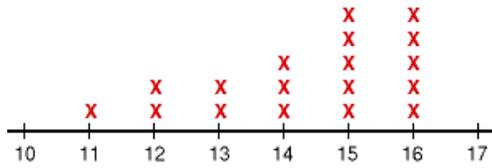
Standard: 3.17 The student will

- a) collect and organize data, using observations, measurements, surveys, or experiments;
- b) construct a line plot, a picture graph, or a bar graph to represent the data; and
- c) read and interpret the data represented in line plots, bar graphs, and picture graphs and write a sentence analyzing the data.

Understanding the Standard Background information of teachers

- Investigations involving data should occur frequently and relate to students' experiences, interests, and environment.
- Formulating questions for investigations is student-generated at this level. For example: What is the cafeteria lunch preferred by students in the class when four lunch menus are offered?
- The purpose of a graph is to represent data gathered to answer a question.
- Bar graphs are used to compare counts of different categories (categorical data). Using grid paper ensures more accurate graphs.
 - A bar graph uses parallel, horizontal or vertical bars to represent counts for categories. One bar is used for each category, with the length of the bar representing the count for that category.
 - There is space before, between, and after the bars.
 - The axis displaying the scale representing the count for the categories should extend one increment above the greatest recorded piece of data. Third grade students should collect data that are recorded in increments of whole numbers, usually multiples of 1, 2, 5, or 10.
 - Each axis should be labeled, and the graph should be given a title.
 - Statements representing an analysis and interpretation of the characteristics of the data in the graph (e.g., similarities and differences, least and greatest, the categories, and total number of responses) should be written.
- A line plot shows the frequency of data on a number line. Line plots are used to show the spread of the data and quickly identify the range, mode, and any outliers.

Number of Books Read



Each x represents one student

- When data are displayed in an organized manner, the results of the investigations can be described and the posed question answered.
- Recognition of appropriate and inappropriate statements begins at this level with graph interpretations.

Topic: Probability and Statistics

Focus: Application of Data and Chance

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.17 The student will

- a) collect and organize data, using observations, measurements, surveys, or experiments;
- b) construct a line plot, a picture graph, or a bar graph to represent the data; and
- c) read and interpret the data represented in line plots, bar graphs, and picture graphs and write a sentence analyzing the data.

Essential Knowledge and Skills	Essential Questions	Essential Understandings All Students should...	Tasks/ Recommended Activities
<p>Essential Vocabulary: line plot; picture graph; bar graph; sample space; data; categories; axis</p>			
<p>The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations to</p> <ul style="list-style-type: none"> • Formulate questions to investigate. • Design data investigations to answer formulated questions, limiting the number of categories for data collection to four. • Collect data, using surveys, polls, questionnaires, scientific experiments, and observations. • Organize data and construct a bar graph on grid paper representing 16 or fewer data points for no more than four categories. • Construct a line plot with no more than 30 data points. • Read, interpret and analyze information from line plots by writing at least one statement. • Label each axis on a bar graph and give the bar graph a title. Limit increments on 	<p>How do you collect, organize, record, and display data?</p> <p>How do you interpret the data you have collected?</p> <p>How does the type of data influence the choice of graph?</p> <p>What conclusions can be drawn from the data?</p> <p>Why are graphs helpful?</p>	<ul style="list-style-type: none"> • Understand how data can be collected and organized. • Understand that data can be displayed in different types of graphs depending on the data. • Understand how to construct a line plot, picture graph, or bar graph. • Understand that data sets can be interpreted and analyzed to draw conclusions. 	

the numerical axis to whole numbers representing multiples of 1, 2, 5, or 10.

- **Read** the information presented on a simple bar or picture graph (e.g., the title, the categories, the description of the two axes).
- **Analyze and interpret** information from picture and bar graphs, with up to 30 data points and up to 8 categories, by writing at least one sentence.
- **Describe** the categories of data and the data as a whole (e.g., data were collected on four ways to cook or prepare eggs — scrambled, fried, hard boiled, and egg salad — eaten by students).
- **Identify** parts of the data that have special characteristics, including categories with the greatest, the least, or the same (e.g., most students prefer scrambled eggs).
- **Select** a correct interpretation of a graph from a set of interpretations of the graph, where one is correct and the remaining are incorrect. For example, a bar graph containing data on four ways to cook or prepare eggs — eaten by students show that more students prefer scrambled eggs. A correct answer response, if given, would be that more students prefer scrambled eggs than any other way to cook or prepare eggs.

2nd Quarter

Topic: Patterns, Functions, and Algebra

Focus: Patterns and Property Concepts

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.19 The student will recognize and describe a variety of patterns formed using numbers, tables, and pictures, and extend the patterns, using the same or different forms.

Understanding the Standard

Background information of teachers

- Exploring patterns requires active physical and mental involvement.
- The use of materials to extend patterns permits experimentation or trial-and-error approaches that are almost impossible without them.
- Reproduction of a given pattern in a different representation, using symbols and objects, lays the foundation for writing numbers symbolically or algebraically.
- The simplest types of patterns are repeating patterns. In each case, students need to identify the basic unit of the pattern and repeat it. Opportunities to create, recognize, describe, and extend repeating patterns are essential to the primary school experience.
- Growing patterns are more difficult for students to understand than repeating patterns because not only must they determine what comes next, they must also begin the process of generalization. Students need experiences with growing patterns in both arithmetic and geometric formats.
- Create an arithmetic number pattern. Sample numeric patterns include
 - 6, 9, 12, 15, 18, ... (growing pattern);
 - 1, 2, 4, 7, 11, 16, ... (growing pattern);
 - 20, 18, 16, 14, ... (growing pattern); and
 - 1, 3, 5, 1, 3, 5, 1, 3, 5 ... (repeating pattern).
- In geometric patterns, students must often recognize transformations of a figure, particularly rotation or reflection. Rotation is the result of turning a figure around a point or a vertex, and reflection is the result of flipping a figure over a line.
- Sample geometric patterns include
 - $\bigcirc \triangle \bigcirc \bigcirc \triangle \triangle \bigcirc \bigcirc \bigcirc \triangle \triangle \triangle \dots$; and
 - $\square \square \star \star \square \star \square \square \star \star \square \star \dots$
- A table of values can be analyzed to determine the pattern that has been used, and that pattern can then be used to find the next value.

Topic: Patterns, Functions, and Algebra

Focus: Patterns and Property Concepts

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.19 The student will recognize and describe a variety of patterns formed using numbers, tables, and pictures, and extend the patterns, using the same or different forms.

Essential Knowledge and Skills	Essential Questions	Essential Understandings All Students should...	Tasks/ Recommended Activities
<p><i>Essential Vocabulary:</i> pattern(s), growing patterns, numeric patterns, geometric patterns</p>			
<ul style="list-style-type: none"> • • The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations to • Recognize repeating and growing numeric and geometric patterns (e.g., skip counting, addition tables, and multiplication tables). • Describe repeating and growing numeric and geometric patterns formed using numbers, tables, and/or pictures, using the same or different forms. • Extend repeating and growing patterns of numbers or figures using concrete objects, numbers, tables, and/or pictures. 	<p>What is the repeating and/or increasing unit in the pattern?</p> <p>Where might we find geometric patterns in real life?</p> <p>What strategies can be used to continue the pattern?</p> <p>What rule can be expressed to describe the pattern?</p>	<ul style="list-style-type: none"> • Understand that numeric and geometric patterns can be expressed in words or symbols. • Understand the structure of a pattern and how it grows or changes. • Understand that mathematical relationships exist in patterns. • Understand that patterns can be translated from one representation to another. 	

Topic: Patterns, Functions, and Algebra

Focus: Patterns and Property Concepts

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.20 The student will

- a) investigate the identity and the commutative properties for addition and multiplication; and
- b) identify examples of the identity and commutative properties for addition and multiplication.

Understanding the Standard

Background information of teachers

- Investigating arithmetic operations with whole numbers helps students learn about several different properties of arithmetic relationships. These relationships remain true regardless of the numbers.
- The commutative property for addition states that changing the order of the addends does not affect the sum (e.g., $4 + 3 = 3 + 4$). Similarly, the commutative property for multiplication states that changing the order of the factors does not affect the product (e.g., $2 \times 3 = 3 \times 2$).
- The identity property for addition states that if zero is added to a given number, the sum is the same as the given number. The identity property of multiplication states that if a given number is multiplied by one, the product is the same as the given number.
- A number sentence is an equation with numbers (e.g., $6 + 3 = 9$; or $6 + 3 = 4 + 5$).

Topic: Patterns, Functions, and Algebra

Focus: Patterns and Property Concepts

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.20 The student will

- a) investigate the identity and the commutative properties for addition and multiplication; and
- b) identify examples of the identity and commutative properties for addition and multiplication.

Essential Knowledge and Skills	Essential Questions	Essential Understandings All Students should...	Tasks/ Recommended Activities
<p><i>Essential Vocabulary:</i> commutative property of multiplication, identity property of multiplication, factors, number sentence</p>			
<p>The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations to</p> <ul style="list-style-type: none"> • Investigate the identity property for multiplication and determine that when the number one is multiplied by another number or another number is multiplied by the number one, that number remains unchanged. Examples of the identity property for multiplication are $1 \times 3 = 3$; $6 \times 1 = 6$. • Recognize that the commutative property for addition is an order property. Changing the order of the addends does not change the sum ($5 + 4 = 9$ and $4 + 5 = 9$). • Recognize that the commutative property for multiplication is an order property. Changing the order of the factors does not change the product ($2 \times 3 = 3 \times 2$). • Write number sentences to represent equivalent mathematical relationships (e.g., $4 \times 3 = 14 - 2$). • Identify examples of the identity and commutative properties for addition and multiplication. 	<p>What is the identity property of multiplication?</p> <p>How can the identity property help solve problems?</p> <p>What is the commutative property?</p> <p>How can the commutative property help solve problems?</p> <p>Why does changing the order of the factors not change the product</p>	<p>The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations to</p> <ul style="list-style-type: none"> • Investigate the identity property for multiplication and determine that when the number one is multiplied by another number or another number is multiplied by the number one, that number remains unchanged. Examples of the identity property for multiplication are $1 \times 3 = 3$; $6 \times 1 = 6$. • Recognize that the commutative property for multiplication is an order property. Changing the order of the factors does not change the product ($2 \times 3 = 3 \times 2$). • Write number sentences to represent equivalent mathematical relationships (e.g., $4 \times 3 = 14 - 2$). 	

		<ul style="list-style-type: none">• Identify examples of the identity and commutative properties for multiplication.	
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Topic: Number and Number Sense

Focus: Place Value and Fractions

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.2 The student will recognize and use the inverse relationships between addition/subtraction and multiplication/division to complete basic fact sentences. The student will use these relationships to solve problems.

Understanding the Standard

Background information of teachers

- Multiplication and division are inverse operations.
- In building thinking strategies for division, an emphasis is placed on connecting the division fact to the related multiplication fact. Building fact sentences helps strengthen this relationship.
- Multiplication and division should be taught concurrently in order to develop understanding of the inverse relationship.

Topic: Number and Number Sense

Focus: Place Value and Fractions

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.2 The student will recognize and use the inverse relationships between addition/subtraction and multiplication/division to complete basic fact sentences. The student will use these relationships to solve problems.

Essential Knowledge and Skills	Essential Questions	Essential Understandings All Students should...	Tasks/ Recommended Activities
<p><i>Essential Vocabulary:</i> inverse operations, multiplication, division,</p>			
<p>The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations to</p> <ul style="list-style-type: none"> Use the inverse relationships between multiplication/division to solve related basic fact sentences. For example: $4 \times 3 = 12$ and $12 \div 4 = \underline{\quad}$. Write three related basic fact sentences when given one basic fact sentence for multiplication/division. For example, given $3 \times 2 = 6$, solve the related facts $\underline{\quad} \times 3 = 6$, $6 \div 3 = \underline{\quad}$, and $6 \div \underline{\quad} = 3$. 	<p>What is an inverse relationship?</p> <p>What are efficient methods for finding products and quotients?</p> <p>Will knowing related multiplication and division facts help you solve problems? Explain your answer.</p>	<p>All students should</p> <ul style="list-style-type: none"> Understand how addition and subtraction are related. Understand how multiplication and division are related. 	

Topic: Computation and Estimation

Focus: Computation and Fraction Operations

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.5 The student will recall multiplication facts through the twelves table, and the corresponding division facts.

Understanding the Standard
Background information of teachers

- The development of computational fluency relies on quick access to number facts.
- A certain amount of practice is necessary to develop fluency with computational strategies; however, the practice must be motivating and systematic if students are to develop fluency in computation, whether mental, with manipulative materials, or with paper and pencil.
- Strategies to learn the multiplication facts through the twelves table include an understanding of multiples/skip counting, properties of zero and one as factors, pattern of nines, commutative property, and related facts.
- In order to develop and use strategies to learn the multiplication facts through the twelves table, students should use concrete materials, hundred chart, and mental mathematics.
- To extend the understanding of multiplication, three models may be used:
 - The equal-sets or equal-groups model lends itself to sorting a variety of concrete objects into equal groups and reinforces repeated addition or skip counting.
 - The array model, consisting of rows and columns (e.g., 3 rows of 4 columns for a 3-by-4 array) helps build the commutative property.
 - The length model (e.g., a number line) also reinforces repeated addition or skip counting.

Topic: Computation and Estimation

Focus: Computation and Fraction Operations

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.5 The student will recall multiplication facts through the twelves table, and the corresponding division facts.

Essential Knowledge and Skills	Essential Questions	Essential Understandings All Students should...	Tasks/ Recommended Activities
<p><i>Essential Vocabulary:</i> multiplication facts, division facts, factor, product, number line,</p>			
<p>The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations to</p> <ul style="list-style-type: none"> • Recall and state the multiplication and division facts through the twelves table. • Recall and write the multiplication and division facts through the twelves table. 	<p>What is a divisor, dividend, and quotient?</p> <p>What are factors and products?</p> <p>Why would someone need to multiply or divide?</p> <p>What are different models for multiplication and division?</p> <p>How can the array model be used to solve multiplication problems?</p> <p>How can a number line reinforce multiplication and division concepts?</p> <ul style="list-style-type: none"> • How can knowledge of equal sharing and forming equal groups help to solve 	<ul style="list-style-type: none"> • Develop fluency with number combinations for multiplication and division. • Understand that multiplication is repeated addition. • Understand that division is the inverse of multiplication. • Understand that patterns and relationships exist in the facts. • Understand that number relationships can be used to learn and retain the facts. 	

	<p>division problems?</p> <p>What strategies can be used to solve multiplication and division problems?</p> <p>How can skip counting help solve multiplication and division problems?</p> <p>What is the product of 7 and 12?</p> <p>Why is 6×4 equal to 12×2?</p> <p>Which method for multiplication works best for you?</p> <p>What is 81 divided by 9?</p> <p>Why does 3×4 equal the same as 2×6?</p> <p>Which method for division works best for you?</p>		
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Topic: Computation and Estimation

Focus: Computation and Fraction Operations

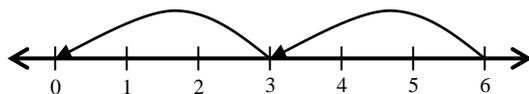
Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.6 The student will represent multiplication and division, using area, set, and number line models, and create and solve problems that involve multiplication of two whole numbers, one factor 99 or less and the second factor 5 or less.

Understanding the Standard

Background information of teachers

- The multiplication and division facts through the twelves tables should be modeled.
- Multiplication is a shortcut for repeated addition. The terms associated with multiplication are listed below:
factor → 54
factor → $\times 3$
product → 162
- Creating real-life problems and solving them facilitates the connection between mathematics and everyday experiences (e.g., area problems).
- The use of Base-10 blocks and repeated addition can serve as a model. For example, 4×12 is read as four sets consisting of one rod and two units. The sum is renamed as four rods and eight units or 48. This can be thought of as
 $12 + 12 + 12 + 12 = (\text{SET})$
- The use of Base-10 blocks and the array model can be used to solve the same problem. A rectangle array that is one rod and two units long by four units wide is formed. The area of this array is represented by 4 rods and 8 units.
- The number line model can be used to solve a multiplication problem such as 3×4 . This is represented on the number line by three jumps of four.
- The number line model can be used to solve a division problem such as $6 \div 3$ and is represented on the number line by noting how many jumps of three go from 6 to 0.



The number of jumps (two) of a given length (three) is the answer to the question.

- An algorithm is a step-by-step method for computing.

Topic: Computation and Estimation

Focus: Computation and Fraction Operations

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.6 The student will represent multiplication and division, using area, set, and number line models, and create and solve problems that involve multiplication of two whole numbers, one factor 99 or less and the second factor 5 or less.

Essential Knowledge and Skills	Essential Questions	Essential Understandings All Students should...	Tasks/ Recommended Activities
<p><i>Essential Vocabulary:</i> multiplication facts, division facts, factor, product, number line</p>			
<p>The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations to</p> <ul style="list-style-type: none"> • Model multiplication, using area, set, and number line models. • Model division, using area, set, and number line models. • Solve multiplication problems, using the multiplication algorithm, where one factor is 99 or less and the second factor is 5 or less. • Create and solve word problems involving multiplication, where one factor is 99 or less and the second factor is 5 or less. 	<p>When would multiplication or division be the appropriate operation to solve a problem?</p> <p>What different strategies can be used to solve multiplication and division problems?</p>	<ul style="list-style-type: none"> • Understand the meanings of multiplication and division. • Understand the models used to represent multiplying and dividing whole numbers. 	

Topic: Number and Number Sense

Focus: Place Value and Fractions

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.3 The student will

- a) name and write fractions (including mixed numbers) represented by a model;
- b) model fractions (including mixed numbers) and write the fractions' names; and
- c) compare fractions having like and unlike denominators, using words and symbols ($>$, $<$, or $=$).

Understanding the Standard Background information of teachers
<ul style="list-style-type: none">• A fraction is a way of representing part of a whole (as in a region/area model or a length/measurement model) or part of a group (as in a set model). Fractions are used to name a part of one thing or a part of a collection of things. Models can include pattern blocks, fraction bars, rulers, number line, etc.• In each area/region and length/measurement model, the parts must be equal-sized (congruent). Wholes are divided or partitioned into equal-sized parts. In the set model, each member of the set is an equal part of the set. The members of the set do not have to be equal in size.• The denominator tells how many equal parts are in the whole or set. The numerator tells how many of those parts are being considered.• Provide opportunities to make connections among fraction representations by connecting concrete or pictorial representations with oral language and symbolic representations.• Informal, integrated experiences with fractions at this level will help students develop a foundation for deeper learning at later grades. Understanding the language of fractions (e.g., <i>thirds</i> means “three equal parts of a whole,” 13 represents one of three equal-size parts when a pizza is shared among three students, or <i>three-fourths</i> means “three of four equal parts of a whole”) furthers this development.• Comparing unit fractions (a fraction in which the numerator is one) builds a mental image of fractions and the understanding that as the number of pieces of a whole increases, the size of one single piece decreases (e.g., 15 of a bar is smaller than 14 of a bar).• Comparing fractions to a benchmark on a number line (e.g., close to 0, less than 12, exactly 12, greater than 12, or close to 1) facilitates the comparison of fractions when using concrete materials or pictorial models.

Topic: Number and Number Sense

Focus: Place Value and Fractions

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.3 The student will
 a) name and write fractions (including mixed numbers) represented by a model;
 b) model fractions (including mixed numbers) and write the fractions' names; and
 c) compare fractions having like and unlike denominators, using words and symbols (>, <, or =).

Essential Knowledge and Skills	Essential Questions	Essential Understandings All Students should...	Tasks/ Recommended Activities
Essential Vocabulary: fraction; parts; set; whole; denominator; like and unlike denominators; numerator; half (halves); third (thirds); fourth (fourths); eighth (eighths); tenth (tenths)			
<ul style="list-style-type: none"> • Name and write fractions (including mixed numbers) represented by a model to include halves, thirds, fourths, eighths, tenths, and twelfths. • Use concrete materials and pictures to model at least halves, thirds, fourths, eighths, tenths, and twelfths. • Compare fractions using the terms greater than, less than, or equal to and the symbols (<, >, and =). Comparisons are made between fractions with both like and unlike denominators, using models, concrete materials and pictures. 	<p>How can you use fractions in real life?</p> <p>How do you identify and record the fraction of a whole or group?</p> <p>How can concrete materials and drawings be used to show an understanding of fractions?</p> <p>Explain the meaning of a fraction and its numerator and denominator?</p> <p>Explain how changing the size of the whole affects</p>	<ul style="list-style-type: none"> • Understand that the whole must be defined. • Understand that the denominator tells the number of equal parts that represent a whole. • Understand that the numerator is a counting number that tells how many equal size parts are being considered. • Understand that the value of a fraction is dependent on both the number of parts in a whole (denominator) and the number of those parts being considered (numerator). 	

	<p>the size or amount of a fraction?</p> <p>How many ways can we use models to determine and compare fractions?</p> <p>What is the difference between a proper and improper fraction?</p> <p>How are improper fractions and mixed numbers related?</p> <p>Is $\frac{2}{3}$ greater or less than $\frac{1}{2}$?</p> <p>Why is $\frac{5}{8}$ greater than $\frac{1}{2}$?</p> <p>How many ways can you show the fraction $\frac{1}{4}$?</p> <p>Which is greater: $\frac{1}{2}$ or $\frac{5}{8}$?</p> <p>Why is $\frac{3}{4}$ greater than $\frac{1}{2}$?</p> <p>How many ways can you show the fraction $\frac{3}{4}$?</p>	<ul style="list-style-type: none"> • Understand that a proper fraction is a fraction whose numerator is smaller than its denominator. • Understand that an improper fraction is a fraction whose numerator is greater than or equal to the denominator and is one or greater than one. • Understand that an improper fraction can be expressed as a whole number or a mixed number. • Understand that a mixed number is written as a whole number and a proper fraction. 	
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Topic: Computation and Estimation

Focus: Computation and Fraction Operations

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.7 The student will add and subtract proper fractions having like denominators of 12 or less. ($>$, $<$, or $=$).

Understanding the Standard

Background information of teachers

- A proper fraction is a fraction whose numerator is less than the denominator. A proper fraction is a fraction that is always less than one.
- An improper fraction is a fraction whose numerator is greater than or equal to the denominator. An improper fraction is a fraction that is equal to or greater than one.
- An improper fraction can be expressed as a mixed number. A mixed number is written as a whole number and a proper fraction.
- The strategies of addition and subtraction applied to fractions are the same as the strategies applied to whole numbers.
- Reasonable answers to problems involving addition and subtraction of fractions can be established by using benchmarks such as 0, $\frac{1}{2}$, and 1. For example, $\frac{3}{5}$ and $\frac{4}{5}$ are each greater than $\frac{1}{2}$, so their sum is greater than 1.
- Concrete materials and pictorial models representing area/regions (circles, squares, and rectangles), length/measurements (fraction bars and strips), and sets (counters) can be used to add and subtract fractions having like denominators of 12 or less.

Topic: Computation and Estimation

Focus: Computation and Fraction Operations

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.7 The student will add and subtract proper fractions having like denominators of 12 or less.

Essential Knowledge and Skills	Essential Questions	Essential Understandings All Students should...	Tasks/ Recommended Activities
<p>Essential Vocabulary: proper fraction; numerator; denominator; improper fraction</p>			
<ul style="list-style-type: none"> • Demonstrate a fractional part of a whole, using <ul style="list-style-type: none"> • region/area models (e.g., pie pieces, pattern blocks, geoboards, drawings); • set models (e.g., chips, counters, cubes, drawings); and • length/measurement models (e.g., nonstandard units such as rods, connecting cubes, and drawings). • Name and write fractions and mixed numbers represented by drawings or concrete materials. • Represent a given fraction or mixed number, using concrete materials, pictures, and symbols. For example, write the symbol for one-fourth and represent it with concrete materials and/or pictures. • Add and subtract with proper fractions having like denominators of 12 or less, using concrete materials and pictorial models representing area/regions (circles, squares, and rectangles), length/measurements (fraction bars and strips), and sets (counters). 	<p>How does fractional computation (add/subtract) relate to whole number computation (add/subtract)?</p> <p>How are models used to show how fractional parts are combined or separated?</p>	<ul style="list-style-type: none"> • Understand that a proper fraction is a fraction whose numerator is smaller than its denominator. • Understand that an improper fraction is a fraction whose numerator is greater than or equal to the denominator and is one or greater than one. • Understand that an improper fraction can be expressed as a whole number or a mixed number. • Understand that a mixed number is written as a whole number and a proper fraction. A mixed number is the sum of a whole number and the proper fraction. • Understand that computation with fractions uses the same strategies as whole number computation. 	

3rd Quarter

Topic: Measurement

Focus: US Customary and Metric Units, Area and Perimeter, and Time

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.11 The student will
a) tell time to the nearest minute, using analog and digital clocks; and
b) determine elapsed time in one-hour increments over a 12-hour period.

Understanding the Standard
Background information of teachers

- While digital clocks make reading time easy, it is necessary to ensure that students understand that there are sixty minutes in an hour.
 - Use of a demonstration clock with gears ensures that the positions of the hour hand and the minute hand are precise when time is read.
 - Students need to understand that time has passed or will pass.
 - Elapsed time is the amount of time that has passed between two given times.
 - Elapsed time should be modeled and demonstrated using geared analog clocks and timelines.
 - It is necessary to ensure that students understand that there are sixty minutes in an hour when using analog and digital clocks.
 - Elapsed time can be found by counting on from the beginning time to the finishing time.
 - Count the number of whole hours between the beginning time and the finishing time.
- For example, to find the elapsed time between 7 a.m. and 10 a.m., students can count on to find the difference between the times (7 and 10), so the total elapsed time is 3 hours.

Topic: Measurement

Focus: US Customary and Metric Units, Area and Perimeter, and Time

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.11 The student will
 a) tell time to the nearest minute, using analog and digital clocks; and
 b) determine elapsed time in one-hour increments over a 12-hour period.

Essential Knowledge and Skills	Essential Questions	Essential Understandings All Students should...	Tasks/ Recommended Activities
<p><i>Essential Vocabulary:</i> analog, digital clocks, elapsed time, periods of time, minutes, hours</p>			
<p>The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations to</p> <ul style="list-style-type: none"> • Tell time to the nearest minute, using analog and digital clocks. • Match the times shown on analog and digital clocks to written times and to each other. • When given the beginning time and ending time, determine the elapsed time in one-hour increments within a 12-hour period (times do not cross between a.m. and p.m.). • Solve practical problems in relation to time that has elapsed. 	<p>Why is telling time important?</p> <p>How is a clock used to tell time to the nearest minute?</p> <p>How can you tell time using digital and analog clock faces?</p> <p>How can you determine how much time has passed between events?</p> <p>How many hours passed from 9:00 to 11:00?</p> <p>Why is 11:00 am different</p>	<ul style="list-style-type: none"> • Apply appropriate techniques to determine time to the nearest minute, using analog and digital clocks. • Understand how to determine elapsed time in one-hour increments over a 12-hour period. 	

	<p>than 11:00 pm?</p> <p>How would you decide if it was am or pm?</p> <p>How many hours have passed from 9:30 to 11:30?</p> <p>Why is 12:00am different from 12:00pm?</p> <p>What would be doing at 8:00pm?</p>		
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Topic: Measurement

Focus: US Customary and Metric Units, Area and Perimeter, and Time

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.12 The student will identify equivalent periods of time, including relationships among days, months, and years, as well as minutes and hours.

Understanding the Standard
Background information of teachers

- The knowledge that a year has 365 and $\frac{1}{4}$ days will help students understand the necessity of adding a full day every fourth year, called a *leap year*.
- The use of a calendar facilitates the understanding of time relationships between days and months, days and weeks, days and years, and months and years. Recognize that students need to know the relationships, such as if there are 24 hours in one day, how many hours are in three days? If the date is January 6, what date would it be in two weeks? How many weeks are in March, April, and May?
- The use of an analog clock facilitates the understanding of time relationships between minutes and hours and hours and days.

Topic: Measurement

Focus: US Customary and Metric Units, Area and Perimeter, and Time

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.12 The student will identify equivalent periods of time, including relationships among days, months, and years, as well as minutes and hours.

Essential Knowledge and Skills	Essential Questions	Essential Understandings All Students should...	Tasks/ Recommended Activities
<i>Essential Vocabulary:</i> calendar, days, months, week, years			
The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations to <ul style="list-style-type: none">Identify equivalent relationships observed in a calendar, including the number of days in a given month, the number of days in a week, the number of days in a year, and the number of months in a year.Identify the number of minutes in an hour and the number of hours in a day.	<p>What are the tools of measuring time and how they are used?</p> <p>How do you use a calendar in daily life?</p> <p>How do the different units of time (minute, day, week, etc.) relate to each other?</p>	<p>Understand the relationship that exists among periods of time, using calendars, and clocks.</p>	

Topic: Measurement

Focus: US Customary and Metric Units, Area and Perimeter, and Time

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.8 The student will determine, by counting, the value of a collection of bills and coins whose total value is \$5.00 or less, compare the value of the bills and coins, and make change.

Understanding the Standard

Background information of teachers

The value of a collection of coins and bills can be determined by counting on, beginning with the highest value, and/or by grouping the coins and bills.

A variety of skills can be used to determine the change after a purchase, including

- counting on, using coins and bills, i.e., starting with the amount to be paid (purchase price), counting forward to the next dollar, and then counting forward by dollar bills to reach the amount from which to make change; and
- mentally calculating the difference.

Topic: Measurement

Focus: US Customary and Metric Units, Area and Perimeter, and Time

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.8 The student will determine, by counting, the value of a collection of bills and coins whose total value is \$5.00 or less, compare the value of the bills and coins, and make change.

Essential Knowledge and Skills	Essential Questions	Essential Understandings All Students should...	Tasks/ Recommended Activities
<p>Essential Vocabulary: coin (coins); bill (bills)</p>			
<ul style="list-style-type: none"> • Count the value of collections of coins and bills up to \$5.00. • Compare the values of two sets of coins or bills, up to \$5.00, using the terms <i>greater than</i>, <i>less than</i>, and <i>equal to</i>. • Make change from \$5.00 or less. 	<p>Why is it important to represent currency amounts in different ways?</p> <p>What strategies could be used to find the change?</p> <p>How can I represent the same amount of money using different combinations of coins and bills?</p> <p>How can I represent various amounts of money using decimal notation and symbols for cents or dollars?</p> <p>How can I create efficient ways for combining coins and making change?</p> <p>How many pennies are in</p>	<ul style="list-style-type: none"> • Understand that a collection of coins and bills has a value that can be counted. • Understand how to make change from \$5.00 or less. 	

	<p>\$1.00?</p> <p>Why might you get change back when buying an item at the store?</p> <p>What are the different ways to make \$0.90?</p> <p>How many quarters are in a dollar?</p> <p>Why is a \$1.00 bill the same as four quarters?</p> <p>What are all the different ways to make \$0.65?</p>		
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Topic: Measurement

Focus: US Customary and Metric Units, Area and Perimeter, and Time

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.9 The student will estimate and use U.S. Customary and metric units to measure

- a) length to the nearest 12-inch, inch, foot, yard, centimeter, and meter;
- b) liquid volume in cups, pints, quarts, gallons, and liters;
- c) weight/mass in ounces, pounds, grams, and kilograms; and
- d) area and perimeter.

Understanding the Standard
Background information of teachers

- Weight and mass are different. Mass is the amount of matter in an object. Weight is determined by the pull of gravity on the mass of an object. The mass of an object remains the same regardless of its location. The weight of an object changes dependent on the gravitational pull at its location. In everyday life, most people are actually interested in determining an object’s mass, although they use the term *weight* (e.g., “How much does it weigh?” versus “What is its mass?”).
- The concept of a standard measurement unit is one of the major ideas in understanding measurement. Familiarity with standard units is developed through hands-on experiences of comparing, estimating, measuring, and constructing.
- Benchmarks of common objects need to be established for each of the specified units of measure (e.g., the mass of a mathematics book is about one kilogram). Practical experience measuring the mass of familiar objects helps to establish benchmarks and facilitates the student’s ability to estimate measures.
- One unit of measure may be more appropriate than another to measure an object, depending on the size of the object and the degree of accuracy desired.
- Correct use of measurement tools is essential to understanding the concepts of measurement.
- Perimeter is the distance around any two-dimensional figure and is found by adding the measures of the sides.
- Area is a two-dimensional measure and is therefore measured in square units.

• Area is the number of square units needed to cover a figure, or more precisely, it is the measure in square units of the interior region of a two-dimensional figure.

Topic: Measurement

Focus: US Customary and Metric Units, Area and Perimeter, and Time

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.9 The student will estimate and use U.S. Customary and metric units to measure

- length to the nearest 12-inch, inch, foot, yard, centimeter, and meter;
- liquid volume in cups, pints, quarts, gallons, and liters;
- weight/mass in ounces, pounds, grams, and kilograms; and
- area and perimeter.

Essential Knowledge and Skills	Essential Questions	Essential Understandings All Students should...	Tasks/ Recommended Activities
<p>Essential Vocabulary: length; centimeter; meter; inch; foot; yard; liquid volume; cups; pints; quarts; gallons; liters; weight/mass; ounces; pounds; grams; kilograms; area; perimeter; U.S. Customary ; metric units</p> <ul style="list-style-type: none"> • Estimate and use U.S. Customary and metric units to measure lengths of objects to the nearest 12 of an inch, inch, foot, yard, centimeter, and meter. • Determine the actual measure of length using U.S. Customary and metric units to measure objects to the nearest 12 of an inch, foot, yard, centimeter, and meter. • Estimate and use U.S. Customary and metric units to measure liquid volume to the nearest cup, pint, quart, gallon, and liter. • Determine the actual measure of liquid volume using U.S. Customary and metric units to measure to the nearest cup, pint, quart, gallon, and liter. • Estimate and use U.S. Customary and metric units to measure the weight/mass 	<p>What is the purpose of standard units of measurement?</p> <p>What tools and units are used to measure the attributes of an object?</p> <p>How are the units of measure within a standard system related?</p> <p>How do you determine the</p>	<ul style="list-style-type: none"> • Understand how to estimate measures of length, liquid volume, weight/mass, area and perimeter. • Understand how to determine the actual measure of length, liquid volume, weight/mass, area and perimeter. • Understand that perimeter is a measure of the distance around a polygon. 	

<p>of objects to the nearest ounce, pound, gram, and kilogram.</p> <ul style="list-style-type: none"> • Determine the actual measure of weight/mass using U.S. Customary and metric units to measure the weight/mass of objects to the nearest ounce, pound, gram, and kilogram. • Estimate and use U.S. Customary and metric units to measure area and perimeter. • Determine the actual measure of area or perimeter using U.S. Customary and metric units. 	<p>appropriate tool and unit when measuring?</p> <p>How do you determine which unit of measurement to use?</p> <p>How can length, mass, and capacity be measured using nonstandard units?</p> <p>How do you determine if an estimate or exact measurement is necessary to solve a problem?</p> <p>What strategies help estimate measurements?</p>	<ul style="list-style-type: none"> • Understand that area is a measure of square units needed to cover a surface. 	
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Topic: Measurement

Focus: US Customary and Metric Units, Area and Perimeter, and Time

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.10 The student will

- a) measure the distance around a polygon in order to determine perimeter; and
- b) count the number of square units needed to cover a given surface in order to determine area.

Understanding the Standard Background information of teachers

- A polygon is a closed plane figure composed of at least three line segments that do not cross. None of the sides are curved.
- Perimeter is a measure of the distance around a polygon and is found by adding the measures of the sides.
- Area is the number of iterations of a two dimensional unit needed to cover a surface. The two-dimensional unit is usually a square, but it could also be another shape such as a rectangle or an equilateral triangle.
- Opportunities to explore the concepts of perimeter and area should involve hands-on experiences (e.g., placing tiles (units) around a polygon and counting the number of tiles to determine its perimeter and filling or covering a polygon with cubes (square units) and counting the cubes to determine its area)

Topic: Measurement

Focus: US Customary and Metric Units, Area and Perimeter, and Time

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.10 The student will
 a) measure the distance around a polygon in order to determine perimeter; and
 b) count the number of square units needed to cover a given surface in order to determine area.

Essential Knowledge and Skills	Essential Questions	Essential Understandings All Students should...	Tasks/ Recommended Activities
<p>Essential Vocabulary: square units; polygon; perimeter; area</p>			
<ul style="list-style-type: none"> • Measure each side of a variety of polygons and add the measures of the sides to determine the perimeter of each polygon. • Determine the area of a given surface by estimating and then counting the number of square units needed to cover the surface. 	<p>What is perimeter? How is it measured?</p> <p>What is area? How is it measured?</p>	<ul style="list-style-type: none"> • Understand the meaning of a polygon as a closed figure with at least three sides. None of the sides are curved and there are no intersecting lines. • Understand that perimeter is a measure of the distance around a polygon. • Understand how to determine the perimeter by counting the number of units around a polygon. • Understand that area is a measure of square units needed to cover a surface. • Understand how to determine the area by counting the number of square units. 	

Topic: Measurement

Focus: US Customary and Metric Units, Area and Perimeter, and Time

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.13 The student will read temperature to the nearest degree from a Celsius thermometer and a Fahrenheit thermometer. Real thermometers and physical models of thermometers will be used.

Understanding the Standard
Background information of teachers

- Estimating and measuring temperatures in the environment in Fahrenheit and Celsius require the use of real thermometers.
- A physical model can be used to represent the temperature determined by a real thermometer.
- The symbols for degrees in Celsius ($^{\circ}\text{C}$) and degrees in Fahrenheit ($^{\circ}\text{F}$) should be used to write temperatures.
- Celsius and Fahrenheit temperatures should be related to everyday occurrences by measuring the temperature of the classroom, the outside, liquids, body temperature, and other things found in the environment.

Topic: Measurement

Focus: US Customary and Metric Units, Area and Perimeter, and Time

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.13 The student will read temperature to the nearest degree from a Celsius thermometer and a Fahrenheit thermometer. Real thermometers and physical models of thermometers will be used.

Essential Knowledge and Skills	Essential Questions	Essential Understandings All Students should...	Tasks/ Recommended Activities
Essential Vocabulary: temperatures; thermometers; Celsius; Fahrenheit			
<ul style="list-style-type: none">• Read temperature to the nearest degree from real Celsius and Fahrenheit thermometers and from physical models (including pictorial representations) of such thermometers.	<p>How do you read a thermometer?</p> <p>What does temperature measure?</p> <p>How are Celsius and Fahrenheit related? How are they different?</p> <p>When is it appropriate to estimate? When is it necessary to measure?</p> <p>What activities are appropriate for estimate/exact numbers?</p>	<ul style="list-style-type: none">• Understand how to measure temperature in Celsius and Fahrenheit with a thermometer.	

4th Quarter

Topic: Geometry

Focus: Properties of congruence and Characteristics of Plane and Solid Figures

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.14

The student will identify, describe, compare, and contrast characteristics of plane and solid geometric figures (circle, square, rectangle, triangle, cube, rectangular prism, square pyramid, sphere, cone, and cylinder) by identifying relevant characteristics, including the number of angles, vertices, and edges, and the number and shape of faces, using concrete models.

Understanding the Standard

Background information of teachers

- The van Hiele theory of geometric understanding describes how students learn geometry and provides a framework for structuring student experiences that should lead to conceptual growth and understanding.
 - **Level 0: Pre-recognition.** Geometric figures are not recognized. For example, students cannot differentiate between three-sided and four-sided polygons.
 - **Level 1: Visualization.** Geometric figures are recognized as entities, without any awareness of parts of figures or relationships between components of a figure. Students should recognize and name figures and distinguish a given figure from others that look somewhat the same (e.g., “I know it’s a rectangle because it looks like a door, and I know that the door is a rectangle.”).
 - **Level 2: Analysis.** Properties are perceived, but are isolated and unrelated. Students should recognize and name properties of geometric figures (e.g., “I know it’s a rectangle because it’s closed, it has four sides and four right angles, and opposite sides are parallel.”).
- A plane geometric figure is any two-dimensional closed figure. Circles and polygons are examples of plane geometric figures.
- Three-dimensional figures are called solid figures or simply solids. Solids enclose a region of space. The interior of both plane and solid figures are not part of the figure. Solids are classified by the types of surfaces they have. These surfaces may be flat, curved, or both.
- The study of geometric figures must be active, using visual images and concrete materials.
- Access to a variety of concrete tools such as graph paper, pattern blocks, geoboards, and geometric solids is greatly enhanced by computer software tools that support exploration.
- Opportunity must be provided for building and using geometric vocabulary to describe plane and solid figures.

- A cube is a solid figure with six congruent square faces and with every edge the same length. A cube has 8 vertices and 12 edges.
 - A cylinder is a solid figure formed by two congruent parallel circles joined by a curved surface.
 - A cone is a solid, pointed figure that has a flat, round face (usually a circle) that is joined to a vertex by a curved surface.
 - A rectangular prism is a solid figure in which all six faces are rectangles with three pair of parallel congruent opposite faces.
 - A sphere is a solid figure with all of its points the same distance from its center.
 - A square pyramid is a solid figure with one square face and four triangular faces that share a common vertex.
 - A face is a polygon that serves as one side of a solid figure (e.g., a square is a face of a cube).
 - An angle is formed by two rays with a common endpoint. This endpoint is called the *vertex*. Angles are found wherever lines intersect. An angle can be named in three different ways by using
 - three letters to name, in this order, a point on one ray, the vertex, and a point on the other ray;
 - one letter at the vertex; or
 - a number written inside the rays of the angle.
 - An edge is the line segment where two faces of a solid figure intersect.
 - A vertex is the point at which two lines, line segments, or rays meet to form an angle. It is also the point on a three dimensional figure where three or more faces intersect.
- Students should be reminded that a solid geometric object is hollow rather than solid. The “solid” indicates a three-dimensional figure.

Topic: Geometry

Focus: Properties of congruence and Characteristics of Plane and Solid Figures

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.14

The student will identify, describe, compare, and contrast characteristics of plane and solid geometric figures (circle, square, rectangle, triangle, cube, rectangular prism, square pyramid, sphere, cone, and cylinder) by identifying relevant characteristics, including the number of angles, vertices, and edges, and the number and shape of faces, using concrete models.

Essential Knowledge and Skills	Essential Questions	Essential Understandings All Students should...	Tasks/ Recommended Activities
<p>Essential Vocabulary: circle; square; rectangle; triangle; solid geometric figure; cube; rectangular prism; square pyramid; sphere; cone; cylinder; plane geometric figures; faces; vertices; edges</p>			
<p>The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations to</p> <ul style="list-style-type: none"> • Identify models and pictures of plane geometric figures (circle, square, rectangle, and triangle) and solid geometric figures (cube, rectangular prism, square pyramid, sphere, cone, and cylinder) by name. • Identify and describe plane geometric figures by counting the number of sides and angles. • Identify and describe solid geometric figures by counting the number of angles, vertices, edges, and by the number and shape of faces. • Compare and contrast characteristics of plane and solid geometric figures (e.g., circle/sphere, square/cube, triangle/square pyramid, and rectangle/rectangular prism), by counting the number of sides, angles, vertices, edges, and the number and shape of faces. • Compare and contrast characteristics of solid geometric figures (i.e., cube, rectangular prism, square pyramid, sphere, cylinder, and cone) to similar objects in everyday life (e.g., a party hat is like a cone). 	<p>Where in the real world can I find shapes?</p> <p>How are geometric properties used to solve everyday problems?</p> <p>In what ways can I match solid geometric figures to real life?</p> <p>How can plane and solid shapes be described?</p>	<ul style="list-style-type: none"> • Understand how to identify and describe plane and solid geometric figures by using relevant characteristics. • Understand the similarities and differences between plane and solid figures. 	

<ul style="list-style-type: none">• Identify characteristics of solid geometric figures (cylinder, cone, cube, square pyramid, and rectangular prism).			
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Topic: Geometry

Focus: Properties of congruence and Characteristics of Plane and Solid Figures

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.1

The student will identify and draw representations of points, line segments, rays, angles, and lines.

Understanding the Standard Background information of teachers

- A point is an exact location in space. It has no length or width. Usually, a point is named with a capital letter.
- A line is a collection of points going on and on in both directions. It has no endpoints. When a line is drawn, at least two points on it can be marked and given capital letter names. The line can also be named with a single, lower-case letter. Arrows must be drawn to show that the line goes on in both directions infinitely.
- A line segment is part of a line. It has two endpoints and includes all the points between those endpoints. The endpoints are used to name a line segment.
- A ray is part of a line. It has one endpoint and continues on and on in one direction.
- Angle rulers may be particularly useful in developing the concept of an angle.
- An angle is formed by two rays having a common endpoint. This endpoint is called the *vertex*. Angles are found wherever lines and line segments intersect. An angle can be named in three different ways by using
 - three letters to name, in this order, a point on one ray, the vertex, and a point on the other ray;
 - one letter at the vertex; or
 - a number written inside the rays of the angle.

Topic: Geometry

Focus: Properties of congruence and Characteristics of Plane and Solid Figures

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.15
The student will identify and draw representations of points, line segments, rays, angles, and lines.

Essential Knowledge and Skills	Essential Questions	Essential Understandings All Students should...	Tasks/ Recommended Activities
Essential Vocabulary: point; space; length; width; line; endpoint; line segment; angle; vertex; ray; angle rulers			
<p>The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations to</p> <ul style="list-style-type: none"> • Identify examples of points, line segments, rays, angles, and lines. • Draw representations of points, line segments, rays, angles, and lines, using a ruler or straightedge. 	<p>How do you classify angles?</p> <p>What is the difference between a point, ray, line, and line segment?</p>	<ul style="list-style-type: none"> • Understand that line segments and angles are fundamental components of plane polygons. • Understand that a line segment is a part of a line, has two end points, and contains all the points between those two endpoints. • Understand that points make up a line. • Understand that a line continues indefinitely in two opposite directions. • Understand that a ray is part of a line, has one endpoint, and continues indefinitely in only one direction. • Understand that an angle is formed by two rays having a 	

		common endpoint.	
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Topic: Geometry

Focus: Properties of congruence and Characteristics of Plane and Solid Figures

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.16

The student will identify and describe congruent and noncongruent plane figures.

Understanding the Standard

Background information of teachers

- Congruent plane figures are figures having exactly the same size and shape. Noncongruent plane figures are figures that are not exactly the same size and shape. Opportunities for exploring figures that are congruent and/or noncongruent can best be accomplished by using physical models.
- Have students identify figures that are congruent or noncongruent by using direct comparisons and/or tracing procedures.

Topic: Geometry

Focus: Properties of congruence and Characteristics of Plane and Solid Figures

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.16
 The student will identify and describe congruent and noncongruent plane figures.

Essential Knowledge and Skills	Essential Questions	Essential Understandings All Students should...	Tasks/ Recommended Activities
Essential Vocabulary: congruent; noncongruent			
<ul style="list-style-type: none"> • Identify examples of congruent and noncongruent figures. Verify their congruence by laying one on top of the other using drawings or models. • Determine and explain why plane figures are congruent or noncongruent, using tracing procedures. 	<p>What strategies can be used to verify symmetry and congruency?</p>	<ul style="list-style-type: none"> • Understand that congruent plane figures match exactly. • Understand that noncongruent plane figures do not match exactly. • Understand that congruent plane figures remain congruent even if they are in different spatial orientations. • Understand that noncongruent plane figures remain noncongruent even if they are in different spatial orientations. 	

Topic: Patterns, Functions, and Algebra

Focus: Patterns and Property Concepts

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.19 The student will recognize and describe a variety of patterns formed using numbers, tables, and pictures, and extend the patterns, using the same or different forms.

Understanding the Standard Background information of teachers

- Exploring patterns requires active physical and mental involvement.
- The use of materials to extend patterns permits experimentation or trial-and-error approaches that are almost impossible without them.
- Reproduction of a given pattern in a different representation, using symbols and objects, lays the foundation for writing numbers symbolically or algebraically.
- The simplest types of patterns are repeating patterns. In each case, students need to identify the basic unit of the pattern and repeat it. Opportunities to create, recognize, describe, and extend repeating patterns are essential to the primary school experience.
- Growing patterns are more difficult for students to understand than repeating patterns because not only must they determine what comes next, they must also begin the process of generalization. Students need experiences with growing patterns in both arithmetic and geometric formats.
- Create an arithmetic number pattern. Sample numeric patterns include
 - 6, 9, 12, 15, 18, ... (growing pattern);
 - 1, 2, 4, 7, 11, 16, ... (growing pattern);
 - 20, 18, 16, 14, ... (growing pattern); and
 - 1, 3, 5, 1, 3, 5, 1, 3, 5 ... (repeating pattern).
- In geometric patterns, students must often recognize transformations of a figure, particularly rotation or reflection. Rotation is the result of turning a figure around a point or a vertex, and reflection is the result of flipping a figure over a line.
- Sample geometric patterns include
 - $\bigcirc \triangle \bigcirc \bigcirc \triangle \triangle \bigcirc \bigcirc \bigcirc \triangle \triangle \triangle \dots$; and
 - $\square \square \star \star \square \star \square \square \star \star \square \star \dots$
 - A table of values can be analyzed to determine the pattern that has been used, and that pattern can then be used to find the next value.

Topic: Patterns, Functions, and Algebra

Focus: Patterns and Property Concepts

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.19 The student will recognize and describe a variety of patterns formed using numbers, tables, and pictures, and extend the patterns, using the same or different forms.

Essential Knowledge and Skills	Essential Questions	Essential Understandings All Students should...	Tasks/ Recommended Activities
<i>Essential Vocabulary:</i> pattern(s), growing patterns, numeric patterns, geometric patterns			
<p>The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations to</p> <ul style="list-style-type: none"> Recognize repeating and growing numeric and geometric patterns (e.g., skip counting, addition tables, and multiplication tables). Describe repeating and growing numeric and geometric patterns formed using numbers, tables, and/or pictures, using the same or different forms. Extend repeating and growing patterns of numbers or figures using concrete objects, numbers, tables, and/or pictures. 	<p>What is the repeating and/or increasing unit in the pattern?</p> <p>Where might we find geometric patterns in real life?</p> <p>What strategies can be used to continue the pattern?</p> <p>What rule can be expressed to describe the pattern?</p>	<ul style="list-style-type: none"> Understand that numeric and geometric patterns can be expressed in words or symbols. Understand the structure of a pattern and how it grows or changes. Understand that mathematical relationships exist in patterns. Understand that patterns can be translated from one representation to another. 	

Topic: Probability and Statistics

Focus: Application of Data and Chance

Process standards: The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations.

Standard: 3.18 The student will investigate and describe the concept of probability as chance and list possible results of a given situation.

Understanding the Standard
Background information of teachers

- A spirit of investigation and experimentation should permeate probability instruction, where students are actively engaged in explorations and have opportunities to use manipulatives.
- Investigation of experimental probability is continued at this level through informal activities using two-colored counters, spinners, and random number generators (number cubes).
- Probability is the chance of an event occurring.
- The probability of an event occurring is the ratio of desired outcomes to the total number of possible outcomes. If all the outcomes of an event are equally likely to occur, the probability of the event = $\frac{\text{number of favorable outcomes}}{\text{total number of possible outcomes}}$.
- The probability of an event occurring is represented by a ratio between 0 and 1. An event is “impossible” if it has a probability of 0 (e.g., the probability that the month of April will have 31 days). An event is “certain” if it has a probability of 1 (e.g., the probability that the sun will rise tomorrow morning).
- When a probability experiment has very few trials, the results can be misleading. The more times an experiment is done, the closer the experimental probability comes to the theoretical probability (e.g., a coin lands heads up half of the time).
- Students should have opportunities to describe in informal terms (i.e., *impossible*, *unlikely*, *as likely as*, *equally likely*, *likely*, and *certain*) the degree of likelihood of an event occurring. Activities should include real-life examples.
- For any event, such as flipping a coin, the equally likely things that can happen are called *outcomes*. For example, there are two equally likely outcomes when flipping a coin: the coin can land heads up, or the coin can land tails up.
- A sample space represents all possible outcomes of an experiment. The sample space may be organized in a list, table, or chart.

Topic: Probability and Statistics

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Essential Knowledge and Skills	Essential Questions	Essential Understandings All Students should...	Tasks/ Recommended Activities
<p><i>Essential Vocabulary:</i> data, categories, outcomes, favorable, outcomes, possible outcomes, impossible, unlikely, equally likely, certain</p>			
<p>The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations to</p> <ul style="list-style-type: none"> • Define probability as the chance that an event will happen. • List all possible outcomes for a given situation (e.g., heads and tails are the two possible outcomes of flipping a coin). • Identify the degree of likelihood of an outcome occurring using terms such as <i>impossible, unlikely, as likely as, equally likely, likely, and certain.</i> 	<p>How is the likelihood of an event determined and described?</p> <p>How is the probability of an event determined and described?</p> <p>What is probability?</p> <p>What terms can be used to describe probability?</p>	<ul style="list-style-type: none"> • Investigate, understand, and apply basic concepts of probability. • Understand that probability is the chance of an event happening. 	

Non-negotiables

Rising fourth graders must know their multiplication facts. They must also know how to read, because their reading level affects math as much as the other subjects.